DHANALAKSHMI SRINIVASAN ENGINEERING COLLEGE-PERAMBALUR-621212

DEPARTMENT OF EEE

EE6601/SOLID STATE DRIVES

III YEAR/VI SEM

UNIT-1-DRIVE CHRACTERSTICS PART-A

I – Unit

1. What is meant by electrical drives? MAY2015, MAY2014,

Systems employed for motion control are called drives. And many employ any of the prime movers such as diesel or petrol engines, as or steam turbines, hydraulic motors and electric motors for supplying mechanical energy for motion control. Drives employing electrical motors are known as electrical drives.

2. What are the three modes of operation for electric drive? NOV2017, MAY2013, NOV2010

Steady state, Acceleration including starting and Deceleration including stopping.

3. What is dynamic torque? NOV2015, MAY2015, MAY2014, MAY2011, MAY2010

Torque component Jdw_m/dt is called the dynamic torque because it is present only during the transient operations.

4. What are the advantages of electrical drives? NOV2012, NOV2011

i) They have flexible control characteristics. The steady state and dynamic characteristics of electrical can be shaped to satisfy load requirements.

ii) Drives can be provided with automatic fault detection system.

- iii) They are available in wide range of torque, speed and power.
- iv) It can operate in all four quadrants of speed-speed plane.

v) Control gear required for speed control, starting and braking is usually simple and easy to operate.

5. List out the various components used in electrical drive systems. MAY2015, MAY2014,

Electrical motors, Power modulator, Sources, Control Unit and sensing unit.

6. What are the applications of electrical drives? NOV2016,

Paper mills, Electric traction, Cement mills and Steel mills.

7. Write the best choice of electric motor for the following application. NOV2016, may2010 1. Pump Load - Single or three phase cage induction motors

- 2. Elevator DC series motor, slip ring induction motor.
- 8. Write the fundamental torque equation for dynamic electric drives.NOV2017

 $T{=}T_{\rm L} + Jdw_{\rm m}/dt$

T= Developed motor torque, N-m.

 T_L = Load torque referred to motor shaft, N-m.

J=Moment of inertia, kg-m².

W_m= Angular velocity of motor shaft, rad /sec.

09. What are the components of load torque? MAY2012, MAY2011

Friction torque, Windage torque and torque required to the useful mechanical work.

10.What are the typical elements of an electric drive?NOV2017

Sources ,Power modulator,Dc motor,Control circuit

PART-B

1. State the essential parts of electrical drive. What are the functions of power modulator? (Nov12,Nov11)



- Modern **power** electronics and **drives** are used in **electrical** as well as mechanical industry.
- The **power** converter or **power modulator** circuits are used with **electrical** motor **drives**, providing either DC or AC outputs, or working from either a DC (battery) supply or from the conventional AC supply.

2. Explain in detail about multi quadrant operations. (Nov17, Nov15, may15, May14,Nov14,may13,Nov13,may12) Four quadrant operation of a drive

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		T

	I quadrant	II quadrant	III quadrant	IV quadrant
Operation of the	The hoisting up	The hoisting up	The downward	The downward
Hoist	of the loaded cage	of the unloaded	motion of the	motion of the
		cage	unloaded cage	loaded cage
T _e	+VE	-VE	-VE	+VE
T _L	-VE	+VE	+VE	-VE

WM	+VE	+VE	-VE	-VE
Power	+VE	-VE	+VE	-VE
Operation of the	forward motoring	Forward Braking	Reverse motoring	Reverse Braking
Drive				

3. What are the different modes of operation of electric drives and explain it(may15,may13) Modes of Operation:

An electrical drive operates in three modes:

- \Box Steady state
- □ Acceleration including Starting
- □ Deceleration including Stopping

$T = T_l + J \frac{d\omega_m}{dt}$

According to the above expression the steady state operation takes place when motor torque equals the load torque. The steady state operation for a given speed is realized by adjustment of steady state motor speed torque curve such that the motor and load torques are equal at this speed.

Change in speed is achieved by varying the steady state motor speed torque curve so that motor torque equals the load torque at the new desired speed. In the figure shown below when the motor parameters are adjusted to provide speed torque curve 1, drive runs at the desired speed wm1. Speed is changed to wm2 when the motor parameters are adjusted to provide speed torque curve 2. When load torque opposes motion, the motor works as a motor operating in quadrant I or III depending on the direction of rotation.

When the load is active it can reverse its sign and act to assist the motion. Steady state

Operation for such a case can be obtained by adding a mechanical brake which will produce a torque in a direction to oppose the motion. The steady state operation is obtained at a speed for which braking torque equal the load torque. Drive operates in quadrant II or IV depending upon the rotation.



Acceleration and Deceleration modes are transient modes. Drive operates in acceleration mode. Whenever an increase in its speed is required. For this motor speed torque curve must be changed so that motor torque exceeds the load torque. Time taken for a given change in speed depends on inertia of motor load system and the amount by which motor torque exceeds the load torque.

Increase in motor torque is accompanied by an increase in motor current. Care must be taken to restrict the motor current within a value which is safe for both motor and power modulator. In applications involving acceleration periods of long duration, current must not be allowed to exceed the rated value. When acceleration periods are of short duration a current higher than the rated value is allowed during acceleration. In closed loop drives requiring fast response, motor current may be intentionally forced to the maximum value in order to achieve high acceleration.

Figure shown below shows the transition from operating point A at speed wm1 to operating point B at a higher speed wm2, when the motor torque is held constant during acceleration. The path consists of AD1E1B. In the figure below, 1 to 5 are motor speed torque curves. Starting is a special case of acceleration where a speed change from 0 to a desired speed takes place. All points mentioned in relation to acceleration are applicable to starting. The maximum current allowed should not only be safe for motor and power modulator but drop in source voltage caused due to it should also be in acceptable limits. In some applications

the motor should accelerate smoothly, without any jerk. This is achieved when the starting torque can be increased step lessly from its zero value. Such a start is known as soft start.



Motor operation in deceleration mode is required when a decrease in its speed is required. According to the equation deceleration occurs when load torque exceeds the motor torque. In those applications where load torque is always present with substantial magnitude, enough deceleration can be achieved by simply reducing the motor torque to zero. In those applications where load torque may not always have substantial amount or where simply reducing the motor torque to zero does not provide enough deceleration, mechanical brakes may be used to produce the required magnitude of deceleration. Alternatively, electric braking may be employed. Now both motor and the load torque oppose the motion, thus producing larger deceleration. During electric braking motor current tends to exceed the safe limit. Appropriate changes are made to ensure that the current is restricted within the safe limit.

Figure shown above shows paths followed during transition from point A at speed wm1

to a point C at a lower speed wm3 .When deceleration is carried out using electric braking at a constant braking torque, the operating point moves along the path AD3E3C. When sufficient load torque is present or when mechanical braking is used the operation takes place along the

Path AD2E2C. Stopping is a special case of deceleration where the speed of a running motor is changed to zero.

4. Derive the condition for steady state stability of equilibrium

point(may16,may14,nov14,may13,nov13,may11,may10)

- Equilibrium speed of a motor load system is obtained when the motor torque, T_e equals the load torque T_l.
- Stable state of equilibrium point
 - The equilibrium point is termed as stable, if the operating point is restored after a small departure from it due to disturbance in the motor or load.
- Unstable state of equilibrium point
 - The equilibrium point is termed as stable, if the operating point will not be restored after a small departure from it due to disturbance in the motor or load.



Mathematical condition for the stability of the equilibrium point

$$\frac{\mathrm{d}\mathrm{T}_{\mathrm{I}}}{\mathrm{d}\omega} - \frac{\mathrm{d}\mathrm{T}_{\mathrm{e}}}{\mathrm{d}\omega} > 0$$

5. Explain the typical load torque characteristics of electrical drives. (may15,nov13,may13,nov12,may11)

Types and Characteristics of Load Torque

Classification of load torques:

1. Active Load torques

2. Passive Load torques

Active Load Torques:

Load torques which has the potential to drive the motor under equilibrium conditions are called active load torques.

Load torques usually retains sign when the drive rotation is changed.

Active Load Torques

Passive Torque:

Load torques which always oppose the motion and change their sign on the reversal of motion are called passive load torques.

Torque due to friction cutting – Passive torque.

Components of load torques:

1. Friction Torque (TF)

The friction torque (TF) is the equivalent value of various friction torques referred to the motor shaft.

2. Windage Torque (Tw)

When a motor runs, the wind generates a torque opposing the motion. This is known as the winding torque.

3. Torque required to do useful mechanical work (Tm)

Nature of the torque depends of type of load.

It may be constant and independent of speed, some function of speed, may be time invariant or time variant.

The nature of the torque may change with the change in the loads mode of operation.

Characteristics of different types of load:

In electric drives the driving equipment is an electric motor.

Selection of particular type of motor driving a m/c is the matching of speed-torque charal of the driven unit and that of the motor.

Different types of loads exhibit different speed torque charal.

· Most of the industrial loads can be classified into the following 4 general categories:

- 1. Constant torque type load.
- 2. Torque proportional to speed (generator type load)
- 3. Torque proportional to square of the speed (fan type load)
- 4. Torque inversely proportional to speed (const power type load)
- 1. Constant Torque Characteristic :



The speed – torque characteristic of this type of load is given by T=K.

Working motor have each mechanical nature of work like shaping, cutting, grinding or sharing, require constant torque irrespective of speed. Similarly cranes during the hoisting. Similarly cranes during the hoisting and conveyors handling constant weight of material / unit,

time also exhibit this type of characteristics.

Torque proportional to speed:



Separately execited dc generators connected to a constant resistance load, eddy current brakes and calendaring m/cs have a speed torque characteristics m/cs have a speed – torque characteristics given by T = Kw.

Torque propositional to square of the speed:



Load Torque Square of speed

 $\mathsf{Example}:\mathsf{Fans}$, Rotary pumps , compressors , ship propellers. The speed – torque characteristics of this type of load is given by

Torque inversely propositional to speed:



- In such types of loads, torque is inversely proportional to speed or load power remains constant.
- Eq: Lathes, boring m/cs, milling m/cs, steel mill colier and electric traction load.
- • This type of characteristics is given by
- Most of the load require extra effort at the time of starting to overcome static friction. In power application it is known as brake away torque and load control engineers call it "stiction". The speed torque characteristics of the load are modified near to zero speed.

6. What are the main factors which decide the choice of electrical drives? Nov17,

Nature of electric supply

- Whether AC or DC supply is to be used for supply
- Nature of the drive
 - Whether the particular motor is going to drive individual machine or a group of machines
 - Capital and running cost
- · Maintenance requirement
- Space ad weight restrictions
- Environment and location
- · Nature of load
- Whether the load requires light or heavy starting torque
- Whether load torque increases with speed remain constant
- Whether the load has heavy inertia which may require longer straight time
- · Electrical characteristics of motor
- Starting characteristics,
- Running characteristics,
- speed control and
- Braking characteristics

Size, rating and duty cycle of motors

Whether the motor is going to the operator for a short time or whether it has to run continuously intermittently or on a variable load cycle

- Mechanical considerations
- Type of enclosures, type of bearings, transmission of drive and Noise level.
- Due to practical difficulties, it may not possible to satisfy all the above considerations.
- In such circumstances, it is the experience and knowledge background which plays a vital role in the selection of the suitable drive.

The following points must be given utmost important for the selection of motor.

The factors are:

- Nature of the mechanical load driven
- Matching of the speed torque characteristics of the motor with that of the load
- Starting conditions of the load.

7. Compare AC and DC drives.may2010&2011

S.No	DC drives	AC drives
1	The power circuit and control circuit is	The power circuit and control circuit is
	simple and inexpensive.	complex.
2	The commutator makes the motor bulky,	These problems are not there motors are
	costly and heavy.	inexpensive, particularly the squirrel cage
		motor.
3	It requires frequent maintenance.	Less maintenance.
4	Power / Weight ratio is small.	Power / Weight ratio is large.

8. Explain in detail about regenerative braking.nov2010

• Working the motor in the generator mode while it is still connected to the supply and mechanical energy is converted to electrical energy and fed back to the supply and hence the



9. Write equations governing DC motor load dynamics.(Nov17,may14,nov14,nov13,nov10)

- 1. DIAGRAM for Motor Load system
- 2. Torque equation for rotational motion
- 3. Governing Equation for Motor-Load system
 - a. Dynamic torque

J= moment of inertia of the motor load reference to the motor shaft Kg-m2 Ω m=

instantaneous angular velocity of the motor shaft, rad/sec T= torque developed in the motor shaft, N-m TL= load torque (resistance) referred to the motor shaft.

- The torque developed in the motor is counter balanced by load torque TL and the dynamic equation $Jd\Omega m/dt$

• Jd Ω m/dt it is present during the transient operation • Drive accelerate are decelerate depend upon weather T is greater than TL during acceleration: motor should drive not only the TL but also additional component Jd Ω m/dt to over come the drive inertia (eg: trains)

$$T = J \frac{\mathrm{d}\Omega_m}{\mathrm{d}t} + T_L$$

10. Derive the dynamic equations of motor load system with rotational motion and translational motion.(Nov2015,may2013,may11)





UNIT-2 CONVERTER /CHOPPER FED DC DRIVES

PART-A

1. Mention the methods to control of the speed of a DC shunt motor.NOV2017,nov16,may15.

- i. Armature control method
- ii. Field Control Method
- iii. Voltage Control Method.

2. What is the function of a freewheeling diode in a phase controlled rectifier? nov15, may14

- 1. Input power factor is improved
- 2. Make the lead current continuous

3. What causes poor input factor in phase controlled DC drives? nov13, may10

The input power factor in the phase controlled rectifier is low when the output voltage is less than

the maximum that is when the firing angle is large is large. When the firing angle increases, the

converter draws more lagging reactive power. Therefore the input factors low.

4. What are the uses of phase controlled rectifiers in DC drives?nov16,may15 Rolling Mills, Paper Mill, Hoists, Printing Presses and Textile Mills

5. What is discontinuous conduction mode?may2013,nov2012

In discontinuous conduction mode, the armature current flows from α to β . At β to $\pi + \alpha$,

there is no armature current. It is the discontinuous conduction mode of operation.

6. What are the advantages of three phase drives over single phase drives? NOV17

- 1. Reducing the armature ripple current 2. The filtering requirement is less
- 3. Armature current is mostly continuous 4. Motor performance is better.

7. List out the drawbacks of rectifier fed DC drive.may16,nov15,may14

- 1. Distortion of Supply.
- 2. Low Power factor.
- 3. Ripple in Motor current.
- 8. What are the methods of armature voltage control DC Motor? NOV2017, nov16, may 15. When the Supply is as,
 - 1. Ward Leonard schemes.
 - 2. Transformer with taps and uncontrolled rectifier bridge.
 - 3. Static ward Leonard scheme (or) Controlled rectifiers.

When the supply is DC,

1. Chopper control

9. What is meant by duty cycle in a chopper circuit? Nov15,may14,nov14

Duty Cycle is defined as the ratio of one time of the chopper to total time period of the chopper.

 $\alpha = \frac{T\infty}{T}$

10. What are the various control strategies for varying duty cycle of the chopper?may2015,nov2011

1. Time Ratio Control (TRC) 2. Current Limit Control (CLC)

PART-B

1) Explain the classification of DC Drives.nov 2010

- 1. Single phase drives
 - a) 1Θ half wave drives
 - b) 1Θ ful wave drives
 - i) 1Θ fully controlled converter fed drives
 - ii) 1 Θ half controlled converter fed drives
 - c) 1Θ dual converter fed drives

2. Three phase drives

- a) 3 Θ half wave drives
- b) 3Θ ful wave drives
 - i) 3Θ fully controlled converter fed drives
 - ii) 3 Θ half controlled converter fed drives

c) $3 - \Theta$ dual converter fed drives

3. DC chopper drives

Classification of chopper fed DC drives:

- 1) First quadrant chopper or type A chopper
- 2) Second quadrant chopper or type B chopper
- 3) Two quadrant type A chopper or type C chopper.
- 4) Four quadrant chopper or type E chopper.

Advantage of DC chopper Drive:

- 1) High efficiency
- 2) Flexibility in controls
- 3) Light weight
- 4) Small size
- 5) Quick response

2. Derive the expression for critical speed which separates the continuous conduction mode from discontinuous conduction mode of operation of $1 \oplus$ fully controlled rectifier for separately executed DC motor.(Nov17,16Nov,15may&Nov,14may&nov,13may&nov,12may&nov)

□ In single phase drives, single phase supply used to drive the motor. The drive has poor speed regulation and it can be overcome by closed loop operation.



continuous

Dis continuous conduction waveforms conduction waveforms

Discontinuous conduction

I) Duty interval $(\alpha \le \omega t \le \beta)$

II) Zero current interval ($\beta \le \omega t \le \pi + \alpha$)

Drive operation is described by the following equation:

$$V_a = R_a i_a + L_a di_a/dt + E = V_m sin\omega t$$
, for
 $\alpha \le \omega t \le \beta$

 $V_a = E$ and $i_a = 0$ for $\beta \le \omega t \le \pi + \alpha$ Let these component represented by a single exponent K $1e^{-t/\zeta}a$ then

$$I_a = (\omega t) = v_m/Z \sin (\omega t - \Theta) - E/R_a + K_1 e^{-t/\zeta} a \text{ for } \alpha \le \omega t \le \sin \beta$$

$$Z = \sqrt{\frac{2}{R_a^2 + (wL_a)^2}}$$
$$\Theta = \tan^{-1} (\omega L_a/R_a)$$

$$I_{a} = (\omega t) = v_{m}/Z \ [\sin (\omega t - \Theta) - \sin (\alpha - \Theta) e^{-(\omega t - \alpha) \cot \Phi}] - E/R_{a} \ [1 - e^{-(\omega t - \alpha) \cot \Phi}],$$

for $\alpha \le \omega t \le \beta$

Since $i_a(\beta) = 0$ then

 $v_m/Z \sin (\beta - \Theta) - E/R_a + [E/R_a - v_m/Z \sin (\alpha - \Phi)] e^{-(\beta - \alpha)cot\Phi} = 0$

Since voltage drop across the armature inductance due to dc component of armature current is zero

$$V_a = E + I_a R_a$$

$$V_{a} = 1/\pi [\int \alpha^{\beta} V_{m} \sin\omega t \ d(\omega t) + \int \alpha^{\alpha +} \pi \ E \ d(\omega t)]$$

= V_m (cos
$$\alpha$$
- cos β)/k($\beta - \alpha$) + ($\pi + \alpha - \beta$)E/ $\pi \omega_m$

= V_m (cos α - cos β)/k($\beta - \alpha$) - $\pi R_a/K^2(\beta - \alpha) T$

 ω_{mc} which separates continuous conduction from discontinuous conduction for a given α as

 $\omega_{mc} = R_a V_m / ZK \sin (\alpha - \Phi) [1 + e^{-\pi \cot \Phi} / e^{-\pi \cot \Phi} - 1]$

Continuous conduction

$$V_a = 1/\pi \int_{\alpha}^{\pi + \alpha} V_m \sin \omega t \ d(\omega t) = 2 \ V_m / \pi$$

 $\cos\alpha \; \omega_m = 2 \; V_m/\pi k \; \cos \alpha \text{-} \; R_a/K^2 \text{T}$

No load speed is given by

 $\omega_{mo} = V_m/k$, for $0 \le \alpha \le \pi/2$

= $V_{m} \sin \alpha/K$, for $\pi/2 \le \alpha \le \pi$

Boundary between continuous and discontinuous conduction shown in the fig



3. Single Phase Half Controlled Bridge Converter Control of DC Separately

Excited Motor.(14may&nov)



Driver circuit



A cycle of motor terminal consist of three intervals

- i) Duty interval ($\alpha \le \omega t \le \pi$)
- ii) Freewheeling interval ($\alpha \le \omega t \le \beta$) : operation governed by the following equation:
- Ia Ra+ La dia/dt+E=0



4.Explain in detail about semiconverter fed dc motor drives.may2010,nov2011



Semi converter with waveform





 D_1, D_2 D_1, D_2

Discontinuous conduction waveforms



(c) Continuous conduction waveforms



During the on period of the transistor, $0 \le t \le t_{on}$, the motor terminal voltage is V. The operation is described by

$$R_{\mathbf{a}} \mathbf{i}_{\mathbf{a}} + L_{\mathbf{\underline{a}}} \frac{\mathbf{d} \mathbf{i}_{\mathbf{a}}}{\mathbf{0} \mathbf{d} \mathbf{t}} + E$$

At t=t_{on} T_r turned off and motor current freewheels through the diode and motor terminal voltage is zero during the interval $t_{on} \le t \le T$, Motor operation during the interval is known as freewheeling interval, is described by

$$R_{\mathbf{a}} \mathbf{i}_{\mathbf{a}} + L_{\mathbf{a}} \frac{\mathbf{d} \mathbf{i}}{\mathbf{0} \mathbf{d} \mathbf{t}} + E$$

Ratio of duty interval t_{on} to chopper period T is called duty ratio or duty cycle (δ). Thus δ = Duty interval/T = t_{on}/T



6. Explain time ratio and current limit control.(2015may&2011nov)

The total **time** period of one cycle of output waveform is constant. The average output voltage is directly proportional to the ON **time** of **chopper**. The **ratio** of ON **time** to total **time** is defined as duty cycle. It can be varied between 0 and 1 or between 0 and 100%



Current Limit Control. In a DC to DC converter, the **current** value varies between the maximum as well as the minimum level of constant voltage. In this method, the DC to DC converter is turned ON & then OFF to confirm that **current** is preserved constantly between the upper limits and also lower limits.



7. Explain the operation of the 2 quadrant chopper fed DC drive system.(2015Nov&may)

- Supply is DC (maybe from rectified-filtered AC, or some other DC sources).
- DC-DC converters (coppers) are used.
- suitable for applications requiring position control or fast response, for example in servo applications, robotics, etc.
- Normally operate at high frequency– the average output voltage response is significantly faster– the armature current ripple is relatively less than the controlled rectifier

• In terms of quadrant of operations, 3 possible configurations are possible:- single quadrant,- twoquadrant and four-quadrant

2 Quadrant DC drives

- FORWARD MOTORING (T1 and D2 operate)
 - T1 on: The supply is connected to motor terminal.
 - T1 off: The armature current freewheels through D2.
 - Va (hence speed) is determined by the duty ratio.

REGENERATION (T2 and D1 operate)

- T2 on: motor acts as a generator
- T2 off:, the motor acting as a generator returns energy to the supply through D2.



8. Explain four quadrant operation of chopper in detail.(2017nov,2016may,2015may&Nov) 4 Quadrant DC drives

• A full-bridge DC-DC converter is used.



9. Draw the power circuit diagram and explain the operation of a 3 \oplus full converter for separately excited DC motor.2016may,2015nov.14nov,13nov,10may



The average motor armature voltage is given by

$$V_a = \frac{3}{\pi} \int_{\frac{\pi}{6} + \alpha}^{\frac{\pi}{2} + \alpha} V_{ab} d(\omega t)$$

In the above substitute $V_{ab} = \sqrt{3}V_m \sin\left(\omega t + \frac{\pi}{6}\right)d(\omega t)$

We have $V_a = \frac{3\sqrt{3}}{\pi} V_m \cos \alpha$

The drive speed is given by

$$V_a = E_b + I_a R_a$$
 Wl

Where
$$E_b = K_a \phi \omega$$

Then
$$V_a = K_a \phi \omega_m + I_a R_a$$

$$\omega_m = \frac{V_a - I_a R_a}{K_a \phi}$$

In separately excited DC motor $K_a \phi I_a = T$

$$\omega_m = \frac{V_a}{K_a \phi} - \frac{R_a}{(K_a \phi)^2} T$$

10. Draw and explain the operation of dual converter fed DC drives.may 2010

This page describes how a separately-excited dc shunt motor can be operated in either direction in either of the two modes, the two modes being the motoring mode and the regenerating mode. It can be seen that the motor can operate in any of the four quadrants and the armature of the dc motor in a fast four-quadrant drive is usually supplied power through a dual converter. The dual converter can be operated with either circulating current or without circulating current. If both the converters conduct at the same time, there would be circulating current and the level of circulating current is restricted by an inductor. It is possible to operate only one converter at any instant, but switching from one converter to the other would be carried out after a small delay. This page describes the operation of a dual converter operating without circulating current.

As shown in Fig. 1, the motor is operated such that it can deliver maximum torque below its base speed and maximum power above its base speed. To control the speed below its base speed, the voltage applied to the armature of motor is varied with the field voltage held at its nominal value. To control the speed above its base speed, the armature is supplied with its rated voltage and the field is weakened. It means that an additional single-phase controlled rectifier circuit is needed for field control. Closed-loop control in the field-weakening mode tends to be difficult because of the relatively large time constant of the field.



Fig. 1: Speed-Torque characteristic

The power circuit of the dual-converter dc drive is shown in Fig. 2.



Each converter has six SCRs. The converter that conducts for forward motoring is called the positive converter and the other converter is called the negative converter. Instead of naming the converters as positive converter and negative converter, the names could have been forward and reverse converters. The field is also connected to a controlled-bridge in order to bring about field weakening.

The circuit shown above can be re-drawn as shown in Fig. 3. Usually an inductor is inserted in each line as shown in Fig. 3 and this inductor reduces the impact of notches on line voltages that occur during commutation overlap notches on line voltages that occur during commutation CIRCUIT OPERATION

The operation of the circuit in the circulating-current free mode is not very much different from that described in the previous pages. In order to drive the motor in the forward direction, the positive converter is controlled. To control the motor in the reverse direction, the negative converter is controlled. When the speed of motor is to be changed fast from a high value to a low value in the forward direction, the conduction has to switch from the positive converter to the negative converter. Then the direction of current flow changes in the motor and it regenerates, feeding power back to the source. When the speed is to be reduced in the reverse direction, the conduction has to switch from the negative converter to the positive converter. It is seen that conduction has to switch from one converter to the other when the direction of motor rotation is to change, so that regeneration can occur. During regenerating torque acts as the breaking torque and the motor decelerates fast.



UNIT-3 INDUCTION MOTOR DRIVES

PART-A

1. What are the different methods of speed control of induction motors? &Advantages of induction

motor drives.17Nov,may13

- 1. Stator voltage control.
- 2. Supply frequency.
- 3. Rotor resistance control.
- 4. Slip power recovery control.
 - More efficient
 - Cheaper
 - light in weight
 - Rugged in construction
 - Require less maintenance
 - It can be operated in dirty and explosive environment
 - •

2. What are the three regions in the speed-torque characteristics of the induction motor?17nov,

- a. Motoring region $(0 \le s \le 1)$
- b. Generating region (s < 0)
- c. Plugging region $(1 \le s \le 2)$ where is the slip.

3. What is meant by soft start?may12,nov10

The AC voltage controllers allow a step less control of supply voltage from zero to rated volt. They are

used for soft start of motors.

4. What is mean by v/f control?nov17&nov11

When the frequency is reduced, the input voltage must be reduced proportionally so as to maintain constant flux. Otherwise the core will get saturated resulting in excessive iron loss and magnetizing current. The maximum torque also remains constant under this condition. This type of control is known as v/f control.

5. What is meant by field – weakening mode operation in the stator frequency control? Nov15&nov16 With constant supply voltage and increased supply frequency operation air gap flux gets reduced.

Therefore during this control induction motor is said to be working in field weakening mode.

6. Define slip power?may16&nov15

The portion of air gap power, which is not converted into mechanical power, is called slip power.

7. What is meant by slip power recovery systems? Nov14&may13

In chopper method of speed control for SRIM, the slip power is wasted in the external resistance and the efficiency also reduced. However, instead of wasting the slip power can be recovered by various schemes for the speed control of slip ring induction motor. This system is called as slip power recovery system.

8. What are the disadvantages of static rotor resistance control? may12&nov11

- 1. Slip power is wasted in the rotor circuit resistance.
- 2. Efficiency is less

9. What is a static Kramer drive?nov10

Static Kramer drive is a one type of slip power is converted into dc by diode bridge rectifier and the dc voltage is converted into ac by line commutated inverter and feedback to the supply. As the slip power can flow only in one direction, static Kramer drive offers speed control below synchronous speed only.

S. No	Voltage source inverter	Current source inverter
1	Input voltage is maintained constant.	Input current is maintained constant.
2	It requires feedback diodes.	It does not require feedback diodes
3	VSI is suitable for multimotor drives	CSI is not suitable for multimotor drives
4	Low cost	High Cost
5	Weight and volume is low	Weight and volume is high
6	Fast dynamic response	Slower dynamic response

10.	Compare	voltage sou	rce and curr	ent source inv	erter fed	drives.17nov
10.	Compare	voltage sou	rce and curr	ent source my	erter leu	urives.1/nov

PART-B

1. Explain the V/F control of induction motor drives with block diagram.(nov17, 14May&Nov,13may)

- If frequency varies Saturation Problems Will occur
- \circ $\;$ To avoid this V/f $\;$ has to maintained at a constant value $\;$
- To avoid Impedance drop at low frequency compensation is necessary (i.e v/f Control)



Implementation of volts/Hz strategy in inverter-fed induction motor drives 2. Explain in detail about energy efficient drives.(16Nov,15Nov)



3. Explain in detail about constant air-gap flux control.(16may,15nov,10nov,may10)



Drive strategy for constant-air gap-flux-controlled induction motor drive

4. Explain the closed loop speed control of CSI fed induction motor drives.(nov15, 14may, 14 Nov)



CSIM drive system with speed control

5. Explain in detail closed loop control of $3\oplus$ IM.Nov17



Closed-loop induction motor drive with constant volts/Hz control strategy

6. Explain the speed control of VSI fed induction motor drives.nov17 Voltage source inverter allows a variable frequency supply to be obtained from a dc supply.

 \Box VSI can be operated as a stepped wave inverter or PWM inverter. When operated as stepped wave inverter, transistors are switched in sequence with time difference.

 \Box Frequency of the inverter operation varied by varying the T and output of the inverter also varied accordingly.



A schematic of the generic inverter-fed induction motor drive



7. Draw and explain the slip power recovery scheme applicable for $3 \oplus$ slip ring induction motor.Nov10&nov11



8. Explain the open loop and closed loop V/F control strategy for the inverter fed induction motor.Nov17&may16

- Can be used for Multi motor Drives
- Load independent Commutation of the Inverter Devices.
- Inverter Frequencies can go up to 1500 Hz.
- Suitable for high speed operation
- Capacity upto 100 KVA
- At very low speed Commutation voltage is also very low. Up to 10% of the Speed is not reliable.
- Speed Range 1:20
- Not suitable for acceleration on Load and Sudden Load Changes
- Dynamic braking can be realized by an additional converter at the line side.
- Low cost with simple control circuit.
- Efficiency is very poor



Features of v/f control

- Best possible utilization of available current capability
- Generate highest possible Torque per Ampere of Stator Current.

9 .Explain static scherbius drive in detail.Nov12



10. Compare slip power recovery scheme with rotor resistance control.Nov11

S.No	Rotor resistance control	Slip power recovery scheme	
1.	Motor speed can be controlled by	Motor speed can be controlled by changing	
	changing the rotor resistance.	the firing angle of the SCRs.	
2.	Slip power is wasted in the external	Slip power is feedback to the supply	
	resistance.		
3.	Efficiency is decreases	Efficiency is increases	
4.	It provides only sub synchronous speed	It provides both sub and super synchronous	
	operation	speed operation	

UNIT-4 SYNCHRONOUS MOTOR DRIVES PART-A

1. Mention the main difference between the wound field and permanent magnet motors. (nov10&nov11)

When a wound filed motor is started as an induction motor, D.C. field is kept off. In case of a permanent magnet motor, the field cannot be 'turned off'.

2. What are the advantages and applications of PMSM? Nov17,

The advantages of PMSM are,

- High efficiency
- High power factor
- Low sensitivity to supply voltage variations

The application of PMSM is that it is preferred of industrial applications with large duty cycle such as pumps, fans and compressors.

3. What are the uses of a hysteresis synchronous motor?may11&nov10

Small hysteresis motors are extensively used in tape recorders, office equipment and fans. Because of the low starting current, it finds application in high inertia application such as gyrocompasses and small centrifuges.

4. Mention the two modes employed in variable frequency control.may14&may12

Variable frequency control may employ and of the two modes. a. True synchronous mode b. Self-controlled mode

5. Which machine is said to be self controlled? may15, may13

A machine is said to be self controlled if it gets its variable frequency from an inverter whose thrusters are freed in a sequence, using the information of rotor position or stator voltages. In the former a rotor position sensor is employed which measures the rotor position with respect to the stator and sends pulses to the thyristors. Thus frequency of the inverter output is decided by the rotor speed.

6. What is Commutator Less Motor (CLM)?13nov

The self controlled motor has properties of a D.C. Motors both under steady state and

Dynamic conditions and therefore is called Commutator less motor (CLM). These machines have better stability behaviors. They do not fall out of step and do not have oscillatory behaviors, as in normal synchronous motors.

7. Give the application of self controlled synchronous motor.15nov

A self controlled synchronous motor is a substitute for a D.C. motor drive and finds application where a D.C. Motor is objectionable due to its mechanical Commutator, which limits the speed range and power output.

8. What are the applications of synchronous motors? nov14

Synchronous motors were mainly used in constant speed applications. The development of semiconductor variable frequency sources, such as inverters and cycloconverters, has allowed their use in draft fane, main line traction, and servo drives.

9. How are the stator and rotor of the synchronous motor supplied?16nov

The stator of the synchronous motor is supplied from a thyristor power converter capable of providing a variable frequency supply. The rotor, depending upon the situation, may be constructed with slip rings, where it conforms to a conventional rotor. It is supplied with D.C. through slip rings. Sometimes rotor may also be free from sliding contacts (slip rings), in which case the rotor is fed from a rectifier rotating with rotor.

10. List out the commonly used synchronous motors in industry.16may

Commonly used synchronous motors are, Wound field synchronous motors. Permanent magnet synchronous motors, Synchronous reluctance synchronous motors. Hysterias motors.

PART-B

1) Explain the concept of open loop V\F control of synchronous motor. (17nov,15may&nov,14may&nov,2012may&nov,2011may&nov)

Open Loop Volts/Hz Control:



Synchronous speed is directly proportional to frequency. So that the rotor always keeps track the changes of speed. Here all the machines are connected in parallel to the same inverter which is response to the command frequency.

• A flux control black is used which changes the stator voltage with frequency so as to constant flux for speed below base speed and constant terminal voltage for speed above

base speed.

Voltage Source inverter Fed Synchronous Motor Drives

- Here the dc link voltage is variable by using phase controlled rectifier. Disadvantage is commutation is difficult at low speed.
- Since the output voltage is square wave, the inverter is called variable voltage inverter

(or) square wave inverter.



2).Current Source Inverter Fed Synchronous Motor Drives



CSI with individual commutation

- When a synchronous motor fed from CSI, the motor currents are quasi square wave if the commutation is instantaneous. Forced commutation is provided in the inverter circuit to extend the speed range from zero to base speed.
- The motor may be operated at UPF. Large inductance present in the DC link which makes the source current fed to the inverter a constant are hence it is a current source inverter.

3.)Cyclo converter Fed Synchronous Motor Drive

- The line voltage can be used to commutate the thyristor of a converter. The machine can be over excited and runs we have load commutated cycloconverter fed synchronous motor.
- A cycloconverter provide high quality output voltage and sinusoidal resulting current.
- Cycloconveter handle power in both directions. The efficiency and dynamic behavior is good. The line power factor is better as the machine power factor can be made unity.



4) Explain self controlled mode of operation of synchronous motor.





Self controlled synchronous motor

- In self control mode, the supply frequency is changed so that the synchronous speed is same as that of the rotor speed. Unlike, Separate control mode where the control inverter frequency is from an independent oscillator
- Here the pulse train from position sensor may be delayed external command.
- The self controlled motor has the properties of a DC motor both under steady state and dynamic conditions and therefore, is called commutator less motor.

5) Explain power factor control of synchronous motor drive.(15may, nov14&may13) Motor power factor control:



- □ The main aim of adjusting power factor to vary the field current.
- □ If the motor is operated at a power factor of unity, the current drawn by it will have the lowest magnitude for a given input and therefore the lowest internal copper loss.
- \Box The motor voltage and current sensed and fed to the power factor calculator.
- \Box It is actual power factor value.
- The computed power factor value is compare against the power factor commanded value by using error detected.
- The error is amplified by the error amplifier, and its output varies the field current power factor confirm to the commanded value.

6) Explain self control technique of synchronous motor with constant margin angle control.

(16nov,15nov&may,14may,12nov&may,2011may)

Constant Marginal Angle Control:



This drive has an outer speed loop and inner current loop. The rotor position sensed by using rotor position encoder.

- The output of comparator fed to the speed controller and current limiter. It generates trigger pulse. If * sets reference for the closed loop control of the field current IF.
- The load commutaed inverter drives are in medium, high power drives.

This drives are used for the starting of large synchronous machines in gas turbine and pumped storage plants.

7) Explain in detail about Microprocessor Based Control of Synchronous Motor.May10



- The microprocessor control offers features, such as improved performance and reliability versatility of the controller, reduced components and reduced manufacturing cost.
- The microprocessor used in the speed control of a synchronous motor has the following functions.
 - 1. It has ensured commutation of inverter during at low speeds.
 - 2. An automatic change over must occur from forced commutation to machine commutation when the motor assumes the capability for machine commutation.
- Proper distribution of firing pulses to the rectifier, inverter and field circuit converter. A microprocessor based speed control system for synchronous motors consists of 1) Power circuit 2) Microprocessor 3) Suitable interface 4)
 Software design

8).Explain Vector Control of Permanent Magnet Synchronous Motor:nov10



- Electromagnetic torque developed due to the interaction of the current carrying conductor and magnetic field.
- In the fig(i) shows the axis is in quadrature with the armature mmf axis. Each and every armature conductor experiences a force which contributes the torque.
- Knowing the values of the desired torque and speed and also the parameters and voltage to which the motor is subjected to it is possible to compute values of id and iq ref for the desired dynamic and steady state performance.
- These currents are compared with actual currents and error values actuate the triggering circuitry which is also influenced by rotor position sensor and speed sensor.



Block diagram vector control of a BLPM SNW motor

9. Explain the closed loop control scheme of adjustable speed synchronous motor drive. (2016&may15)

Synchronous speed is directly proportional to frequency, similar ti induction motors constant flux operation below base speed is achieved by operating the synchronous motor with constant (V / f) ratio.

The synchronous motor either run at synchronous speed (or) it will not run at all. Hence variable frequency control may employ any of the following two modes

1.True synchronous mode

2.Separate controlled mode





Here all the machines are connected in parallel to the same inverter and they move in response to the command frequency f* at the input. The frequency command f* after passing through the delay circuit is applied to the voltage source inverters (or) a voltage fed PWM inverter. This is done so that the rotor source is able to track the change in frequency.

Self controlled synchronous motor Drive empolying load commuated Thyristor

In fig wound field synchronous motor is used for large power drives.Permanent magnet synchronous motor is used for medium power drives.This drive consists of two converters.i.e source side converter and load side converter.

The source side converter is a 3 phase 6 pulse line commutated fully controlled rectifier .When the firing angle range $0 \le \pm s \le 90^\circ$, it acts as a commutated fully controlled rectifier.



10. Explain the construction and operation of permanent magnet synchronous motor in retail. (17nov,16may,15nov,14nov&may,13nov&may,12nov&may,10may)

PERMANENT MAGNET SYNCHRONOUS MOTOR

- The notation for PMSM is PMAC
- In PMSM the D.C field winding of the rotor is replaced by Permanent Magnets
- Permanent Magnet Materials: Alnico, Cobalt-Samarium, Ferrite.

Advantages:

- Elimination of field copper loss.
- Higher power density.
- Lower rotor inertia.
- More robust construction of motor.
- Higher efficiency.





Disadvantages :

- □ Loss of flexibility of field flux control.
- □ Remagnetization effect.
- \square Higher costs.

UNIT-5 DESIGN OF CONTROLLER

PART-A

1. What is a closed loop control system?may13

A closed loop control system operation is mainly used to maintain constant speed operation. For example an electric drive requires constant speed operation the firing angle has to change to maintain a constant speed. This can be achieved in a closed loop control system.

2. What are the advantages of closed loop speed control?nov15&may14

System protection, Greater accuracy, Improved dynamic response and reduced effects of

disturbances such as loading.

3. What are the two types of feedback in dc drives?

Current feedback and speed feedback.

4. What is speed feedback?17nov

The motor speed can be sensed by any one speed sensor and this signal is compared with

reference speed. This error signal is given to speed controller. The speed controller produce control

signal to the power converter.

5. What are the two types of speed controller?nov12

P controller and PI controller

6. What is current feedback?nov15

The motor current can be sensed by current transducer. This signal is compared with

reference signal. The error signal is fed to the current controller. The current controller produces a

control signal. This signal is fed to the power converter for controlling the output.

7. What are the design procedures for a closed loop speed control system?may14

Assuming that the feedback gains K_t and K_r fixed.

Clamping value of E_i also must be chosen

Calculate current controller gain K_I

Calculate speed controller gain Ks

8. What is armature voltage control?nov16

The dc motor speed can be varied by varying armature voltage and fixed voltage is constant. This voltage can be varied by using power converter. This method only applicable for

below base speed.

9. What is field weakening mode control?may15,nov13

The dc motor speed can be varied by varying the field current and armature voltage is kept constant. The field current can be controlled by using power converter. By using this method the motor field flux decreases ie, field weakening mode. Is method only applicable for above speed because speed is inversely proportional to flux.

10. What are the functions of feedback loops in an electrical drives?nov11

Protection, Improvement of speed response and to improve steady state accuracy.

PART-B

1. Derive the transfer function of separately excited dc motor.(17nov,16may,15nov,14nov)



$$v_{t} = R_{a}i_{a} + L\frac{di_{a}}{dt} + e_{a}$$

 $Te = k_t \phi i_a$

Electric torque

 $e_a = k_E \phi \omega$ Armature back e.m.f.

Armature circuit:

$$V_t = R_a i_a + L \frac{di_a}{dt} + e_a$$

In steady state,

$$\mathbf{V}_{\mathbf{t}} = \mathbf{R}_{\mathbf{a}}\mathbf{I}_{\mathbf{a}} + \mathbf{E}_{\mathbf{a}}$$

Therefore speed is given by,

$$\omega = \frac{V_{t}}{k_{T}\phi} - \frac{R_{a}T_{e}}{(k_{T}\phi)^{2}}$$

Three possible methods of speed control:

Field flux Armature voltage V_t Armature resistance Ra

Derivation of Transfer Functions



$$\underbrace{R(s)}_{H(s)} \xrightarrow{P(s)}_{H(s)} G_{2}(s) \xrightarrow{Y(s)}_{R(s)} \frac{Y(s)}{R(s)} = \frac{G_{1}(s)G_{2}(s)}{1 + G_{1}(s)G_{2}(s)H(s)} \\
 \underbrace{Y(s)}_{D(s)} \xrightarrow{Y(s)}_{D(s)} = \frac{G_{2}(s)}{1 + G_{1}(s)G_{2}(s)H(s)}$$

2.Design procedure of speed control? (17Nov,16may,15nov)



- P controller
- PI controller

3. Draw the circuit diagram and explain the operation of closed loop control with innercurrent loop and field weakening?(nov16,may14)



The motor is driving a load which is proportional to friction. The output of the tachogenerator is filtered to remove the ripples to provide the feedback signal, ω_{mr} . The speed signal (ω_{r}^*) is feedback signal which is compared with the speed command (ω_{mr}) to produce a speed error signal. This signal is processed through a Proportional plus Integral (PI) controller to determine the torque command (T_e^*). The torque command is limited, to keep it within the safe current limits and the current command is obtained by proper scaling. The armature current loop signal i_a^* is compared to the feedback armature current i_a to have a zero current error. If there is an error, a PI current controller processes it to alter the control signal V_c . The control signal accordingly modifies the triggering angle α to be set to the converter for implementation. The inner current loop ensures a fast current response and also limits the current to a safe preset level. This inner current loop makes the converter a linear current amplifier. The outer speed loop ensures that the actual speed is always equal to the commanded speed and that any transient is overcome within the shortest feasible time without exceeding the motor and converter capacity. The operation of closed loop speed controlled drive is explained from one or two particular instances of speed command. A speed from zero to rated value is obtained and the motor is assumed to be at standstill which will generate a large speed error and a torque command and in turn an armature current command. The armature current error will generate the triggering angle to supply a preset maximum dc voltage across the motor terminals.

The inner current loop will maintain the current at a level permitted by its command value, producing a corresponding torque. As the motor starts running, the torque and current are maintained at their maximum level, thus accelerating the motor rapidly. When the rotor attains the command value, the torque command will settle down to a value equal to the sum of load torque and other motor losses to keep the motor performance in steady state. The design of the gain and time constant of the speed and current controllers is of paramount importance in meeting the dynamic specifications of the motor drives. 4. Show the block diagram of a closed loop speed control system DC motor speed control system? (nov16&nov15,may14)



- □ The converters are made up of semiconductor materials, which have low thermal capacity.
- □ DC motor can carry 2 to 3 times of rated current.
- □ Converter and motor is chosen with equal current to allow the maximum permissible rated current.
- □ The above diagram shows the closed loop control with inner current loop control and outer speed control loop.
- \square Basic approach for the closed loop control is above and below the base speed.
- □ The field current is constant and armature voltage is variable for below the base speed and for above base speed field current is variable and armature current is constant.
- \Box The emf is chosen as 0.85 or 0.95 of the rated armature voltage. The speed will be very and it will be compared with reference speed and then speed will be

increased according to reference speed

5. Explain in detail design of current controller of closed loop speed control system of DC separately excited motor.(NOV17,NOV15,MAY14)

Cascade control structure



- The control variable of inner loop (e.g. torque) can be limited by limiting its reference value
- It is flexible outer loop can be readily added or removed depending on the control requirements

Procedure

- Design the torque loop (fastest) first.
- Design the speed loop assuming the torque loop

to be ideal.

• Design the position loop (slowest) assuming the

speed loop to be ideal.

6. Derive the transfer function of DC motor load system with armature voltage control? (nov17,may14,may13,nov12)



$$i_{a}(s) = \frac{1/R_{a}}{1+s\frac{L_{a}}{R_{a}}} \left[\mathsf{v}_{a}(s) - k_{\phi} \, \boldsymbol{\omega}_{\mathbf{m}}(s) \right]$$

$$T_e(s) = k_{\phi} i_a(s)$$

$$\omega_{\rm m}(s) = \frac{T_e(s) - T_L(s)}{sJ}$$

Armature time constant

$$\tau_a = \frac{L_a}{R_a}$$

Electromechanical time constant

$$\tau_m = \frac{JR_a}{k_{\phi}^2}$$



The speed is directly proportional to the voltage applied across the armature. As the supply voltage is normally constant, the voltage across the armature can be controlled by adding a variable resistance in series with the armature as shown in the Fig. 1.



7.. Derive the transfer function of the speed controller?(2016may,2015may,2014may,2013nov)



$$\frac{N(s)}{E_r(s)} = \frac{G(s)}{1 + G(s)H(s)}$$

$$G(s) = K_s K_c \frac{K_{m1}(1 + s\tau_m)}{1 + s\tau_{m1}} \frac{K_{m2}}{1 + s\tau_m}$$

$$G(s) = \frac{K_s K_c K_{m1} K_{m2}}{1 + s\tau_{m1}}$$

$$H(s) = K_t$$

$$\frac{I_{a}(t)}{I_{a}(\infty)} = \frac{\frac{E_{r}K_{1}}{K_{m2}} \left[1 + \frac{\tau_{m} - \tau_{1}}{\tau_{1}} e^{\frac{-t}{\tau_{1}}} \right]}{\frac{E_{r}K_{1}}{K_{m2}}}$$
$$\frac{I_{a}(t)}{I_{a}(\infty)} = 1 + \frac{\tau_{m} - \tau_{1}}{\tau_{1}} e^{-t/\tau_{1}}$$

8. Explain in detail about closed loop armature and field weakening mode in speed control of dc motor.(nov15&may14,may12)



- Converter and motor is chosen with equal current to allow the maximum permissible rated current.
- The above diagram shows the closed loop control with inner current loop control and outer speed control loop.
- Basic approach for the closed loop control is above and below the base speed.
- The field current is constant and armature voltage is variable for below the base speed and for above base speed field current is variable and armature current is constant.

9. Give the design procedure of current controller?(nov17,may15,may13)



10. Converter selection and characteristics (17nov, 15may, 13nov, 12nov, 11nov)

$$I_{rms} = \frac{I_{max}}{\sqrt{3}} = 0.577 I_{max}$$

$$I_{1} = \frac{1}{\sqrt{2}} \cdot \frac{2\sqrt{3}}{\pi} I_{max} = \frac{\sqrt{2}\sqrt{3}}{\pi} I_{max} = 0.78 I_{max}$$

$$P_{0} = V_{a}I_{max}$$

$$= (1.35 \text{ V} \cos \alpha) I_{max}$$

$$= 1.35 \text{ V} I_{max} \cos \alpha$$

$$P_{0} = P_{x} = 1.35 \text{ V} I_{max} \cos \alpha$$

$$I_{max} = \frac{I_{1}}{0.078} = 1.282 I_{1}$$

$$P_{i} = P_{0} = \sqrt{3} \text{ V} I_{1} \cos \alpha$$

$$Q_{i} = \sqrt{3} \text{ V} I_{1} \sin \alpha = 1.35 \text{ V} I_{max} \sin \alpha$$

$$P_{VA} = \sqrt{(P_{i})^{2} + (Q_{i})^{2}} = 1.35 \text{ V} I_{max} = \sqrt{3} \text{ V} I_{1}$$